

DO NOW

pg 99; 36

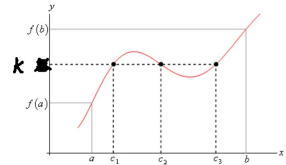
Page 1

2.4 Continuity & One-Sided Limits - Day 3

Intermediate Value Theorem:

If f is continuous on $[a, b]$ and k is any number between $f(a)$ and $f(b)$, then there is at least one number c in $[a, b]$ such that $f(c) = k$.

* maybe more than one value for c



Page 2

Example - A person's height:

↳ is a continuous function

* If some is 5' tall one year and 5'6" 2 years later....

Then they must have been 5'2" at some point

Page 3

Example - A person's bank account:

↳ is not continuous

* When there is a deposit or withdraw there is a "jump" in the function.

* If you start with \$50 and end with \$200

There is no guarantee that \$100 was ever the balance.

Page 4

Intermediate Value Theorem can be used to:

guarantee the existence of at least one zero on an interval.

Suppose $P(a)$ and $P(b)$ are: opposite signs
(one positive and one negative)
* Continuous function
Then the function must have at least one zero.

Bisection Method:

To approximate a zero -
Keep cutting the interval in half
to locate the zero

Page 5

Example:

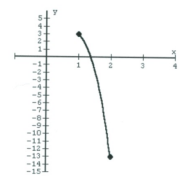
$$f(x) = -x^4 - x + 5$$

$$\text{let } a = 1 \text{ and } b = 2$$

$$f(a) = -1^4 - 1 + 5 = 3$$

$$f(b) = -2^4 - 2 + 5 = -13$$

By the intermediate value theorem,
∴ $[1, 2]$ must have at least one zero
because $f(1)$ is positive and $f(2)$ is negative.
 $x \approx 1.3794$



Page 6

Examples: pg 100; 66

$$g(x) = \begin{cases} \frac{x^2 - a^2}{x - a} & x \neq a \\ 8 & x = a \end{cases}$$

$$\lim_{x \rightarrow a} \frac{x^2 - a^2}{x - a} = 8$$

$$\lim_{x \rightarrow a} \frac{(x-a)(x+a)}{x-a}$$

$$\lim_{x \rightarrow a} (x+a)$$

$$a+a$$

$$2a = 8$$

$$a = 4$$

$$f(a) = \lim_{x \rightarrow a} f(x)$$

$$f(a) = 8$$

HOMEWORK

pg 99 - 102; 63 - 69 odd, 75, 76, 83, 84,
91, 95, 103, 108

92,